

INVENTORS: Urbain Alfred von der Embse

TECHNICAL FIELD

The present invention relates to CDMA (Code Division Multiple Access) cellular telephone and wireless data communications with data rates up to multiple T1 (1.544 Mbps) and higher (>100 Mbps), and to optical CDMA with data rates in the Gbps and higher ranges. Applications are mobile, point-to-point and satellite communication networks. More specifically the present invention relates to novel complex and hybrid complex Walsh codes developed to replace current real Walsh orthogonal CDMA channelization codes.

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BACKGROUND ART

Current art is represented by the recent work on multiple access for broadband wireless communications, the G3 (third generation CDMA) proposed standard candidates, the current IS-95 CDMA standard, the early Qualcomm patents, and the real Walsh technology. These are documented in references 1,2,3,4,5,6. Reference 1 is an issue of the IEEE communications magazine devoted to multiple access communications for broadband wireless

networks, reference 2 is an issue on IEEE personal communications devoted to the third generation (3G) mobile systems in Europe, reference 3 is the IS-95 standard primarily developed by Qualcomm, references 4 and 5 are Qualcomm patents addressing the use of real Walsh orthogonal CDMA codes, and reference 6 is the widely used reference on real Walsh technology.

orthogonal Current art usina real Walsh CDMA channelization codes is represented by the scenario described in the following with the aid of equations (1) and FIG 1,2,3,4. This scenario considers CDMA communications spread over a common frequency band for each of the communication channels. CDMA communications channels for each of the users are defined by assigning a unique Walsh orthogonal spreading codes to each user. The Walsh code for each user spreads the user data symbols over the common frequency band. These Walsh encoded user signals are summed and re-spread over the same frequency band by one or more PN codes, to generate the CDMA communications signal which is The communications link consists of modulated and transmitted. a transmitter, propagation path, and receiver, as well as interfaces and control.

It is assumed that the communication link is in the communications mode with all of the users communicating at the same symbol rate and the synchronization is sufficiently accurate and robust to support this communications mode. In addition, the possible power differences between the users is assumed to be incorporated in the data symbol amplitudes prior to the CDMA encoding in the CDMA transmitter, and the power is uniformly spread over the wideband by proper selection of the CDMA pulse waveform. It is self evident to anyone skilled in the CDMA communications art that these communications mode assumptions are both reasonable and representative of the current CDMA art and do not limit the applicability of this invention.

Transmitter equations (1) describe a representative real Walsh CDMA encoding for the transmitter in FIG. 1. It is assumed that there are N Walsh code vectors W(u) each of length N

The code vector is presented by a 1xN N-chip row chips vector W(u) = [W(u,1),...,W(u,N)] where W(u,n) is chip n of code u. The code vectors are the row vectors of the Walsh matrix W. Walsh code chip n of code vector u has the possible values W(u,n) = +/-1. Each user is assigned a unique Walsh code which allows the code vectors to be designated by the user symbols u=0,1,...,N-1 for N Walsh codes. User data symbols 2 are the set of complex symbols $\{Z(u), u=0, 1, ..., N-1\}$ and the set of real (R(u_R), I(U_I), u_R , u_I =0,1,...,N-1} where Z is a complex symbol and R,I are real symbols assigned to the real, imaginary communications axis. Examples of complex user symbols are QPSK and OOPSK encoded data corresponding to 4-phase and offset 4phase symbol coding. Examples of real user symbols are PSK and DPSK encoded data corresponding to 2-phase and differential 2phase symbol coding. Although not considered in this example, it is possible to use combinations of both complex and real data symbols.

Current real Walsh CDMA encoding for transmitter (1)

- 1 Walsh codes
 - W = Walsh NxN orthogonal code matrix consisting of N rows of N chip code vectors
 - = [W(u)] matrix of row vectors W(u)
 - = [W(u,n)] matrix of elements W(u,n)
 - W(u) = Walsh code vector u for u=0,1,..., N-1
 - = [W(u,0), W(u,1), ..., W(u,N-1)]
 - = 1xN row vector of chips W(u, 0), ..., W(u, N-1)
 - W(u,n) = Walsh code u chip n
 - = +/+1 possible values
- 2 Data symbols
 - Z(u) = Complex data symbol for user u
 - $R(u_R)$ = Real data symbol for user u_R assigned to the real axis of the CDMA signal
 - $I\left(u_{I}\right)$ = Real data symbol for user u_{I} assigned to the imaginary axis of the CDMA signal

3 Walsh encoded data

Complex data symbols

$$Z(u,n) = Z(u) sgn\{ W(u,n) \}$$

= User u chip n Walsh encoded complex data

Real data symbols

$$R(u_R, n) = R(u_R) \operatorname{sgn} \{ W(u_R, n) \}$$

= User u_R chip n Walsh encoded real data

$$I(u_I,n) = R(u_R) sgn\{ W(u_R,n) \}$$

= User u_I chip n Walsh encoded real data

where sgn{ (o) } = Algeraic sign of "(o)"

4 PN scrambling

 $P_{R2}(n)$, $P_{R}(n)$ = Chip n of PN codes for real axis

 $P_{12}(n)$, $P_{1}(n)$ = Chip n of PN codes for imaginary axis

Complex data symbols:

Z(n) = PN scrambled real Walsh encoded data chips
 after summing over the users

$$= \sum_{u} Z(u,n) [P_{R}(n) + j P_{I}(n)]$$

$$= \sum_{n} Z(u,n) \left[\operatorname{sgn} \{ P_{R}(n) \} + j \operatorname{sgn} \{ P_{I}(n) \} \right]$$

= Real Walsh CDMA encoded complex chips

Real data symbols:

$$Z(n) =$$

$$\left[\sum_{u_{R}} R(u_{R}, n) \operatorname{sgn}(P_{R2}(n)) + j\sum_{u_{I}} I(u_{I}, n) \operatorname{sgn}(P_{I2}(n))\right] \left[\operatorname{sgn}\{P_{R}(n)\} + j\operatorname{sgn}\{P_{I}(n)\}\right]$$

= Real Walsh CDMA encoded real chips

User data is encoded by the Walsh CDMA codes 3. Each of the user symbols Z(u), $R(u_R)$, $I(u_I)$ is assigned a unique Walsh code W(u), $W(u_R)$, $W(u_I)$. Walsh encoding of each user data symbol generates an N-chip sequence with each chip in the sequence consisting of the user data symbol with the sign of the corresponding Walsh code chip, which means each chip = [Data symbol] x [Sign of Walsh chip].

The Walsh encoded data symbols are summed and encoded with PN codes 4. These PN codes are 2-phase with each chip equal to

+/-1 which means PN encoding consists of sign changes with each sign change corresponding to the sign of the PN chip. Encoding with PN means each chip of the summed Walsh encoded data symbols has a sign change when the corresponding PN chip is remains unchanged for +1 values. This operation is described by a multiplication of each chip of the summed Walsh encoded data symbols with the sign of the PN chip. Purpose of the PN encoding for complex data symbols is to provide scrambling of the summed Walsh encoded data symbols as well as isolation between groups of Purpose of the separate PN encoding for the real and imaginary axes is to provide approximate orthogonality between the real and imaginary axes, since the same Walsh orthogonal codes are being used for these axes. Another PN encoding can be used as illustrated in these equations for the combined real and imaginary CDMA signals to provide scrambline and isolation between groups of users.

Receiver equations (2) describe a representative real Walsh CDMA decoding for the receiver in FIG. 3. The receiver front end 5 provides estimates $\{\hat{Z}(n) = \hat{R}(n) + j \; \hat{I}(n)\}$ of the transmitted real Walsh CDMA encoded chips $\{Z(n) = R(n) + j I(n)\}$ for the complex and real data symbols. Orthogonality property 6 is expressed as a matrix product of the real Walsh code chips or equivalently as a matrix produce of the Walsh code chip numerical signs. The 2-phase PN codes 7 have the useful decoding property that the square of each code chip is unity which is equivalent to observing that the square of each code chip numerical sign is unity. Decoding algorithms 8 perform the inverse of the signal processing for the encoding in equations (1) to recover estimates $\{\hat{Z}(u)\}$ or $\{\hat{R}(u_R),\; \hat{I}(u_I)\}$ of the transmitter user symbols $\{Z(u)\}$ or $\{R(u_R),\; I(u_I)\}$ for the respective complex or real data symbols.

Current real Walsh CDMA decoding for receiver (2)

5 Receiver front end provides estimates $\{\hat{Z}(n) = \hat{R}(n) + j\hat{I}(n)\}$ of the encoded transmitter chip symbols $\{Z(n) = R(n) + jI(n)\}$

for the complex and real data symbols

6 Orthogonality property of real Walsh NxN matrix W

$$\sum_{n} W(\hat{u}, n) W(n, u) = \sum_{n} \operatorname{sgn}\{W(\hat{u}, n)\} \operatorname{sgn}\{W(n, u)$$
$$= N \delta(\hat{u}, u)$$

where $\delta(\hat{u},\,u)$ = Delta function of \hat{u} and u = 1 for \hat{u} = u

= 0 otherwise

7 PN decoding property

$$P(n) P(n) = sgn\{P(n) \ sgn\{P(n)\}\}$$

8 Decoding algorithm

Complex data symbols

$$\hat{Z}(u) = N^{-1} \sum_{n} \hat{Z}(n) [sgn\{P_{R}(n)\} - j sgn\{P_{I}(n)\}] sgn\{W(n, u)\}$$

= Receiver estimate of the transmitted complex
data symbol Z(u)

Real data symbols

$$\hat{R}(u_R) =$$

Real[$N^{-1} \sum_{n} \hat{Z}(n) [sgn\{P_{R}(n)\} - j sgn\{P_{I}(n)\}] sgn\{P_{R2}(n)\} sgn\{W(n,u_{R})\}$]

= Receiver estimate of the transmitted complex data symbol $R(u_R)$

$$\hat{I}(u_i) =$$

Imag[$N^{-1} \sum_{n} \hat{Z}(n) [sgn\{P_{R}(n)\} - j sgn\{P_{I}(n)\}] sgn\{P_{I2}(n)\} sgn\{W(n,u_{I})\}]$

= Receiver estimate of the transmitted complex data symbol $I\left(u_{\mathrm{I}}\right)$

FIG. 1 CDMA transmitter block diagram is representative of a current CDMA transmitter which includes an implementation of the current real Walsh CDMA channelization encoding in equations (1). This block diagram becomes a representative implementation of the CDMA transmitter which implements the new complex Walsh CDMA encoding when the current real Walsh CDMA encoding 13 is

replaced by the new complex Walsh CDMA encoding of this invention. Signal processing starts with the stream of user input data words 9. Frame processor 10 accepts these data words and performs the encoding and frame formatting, and passes the outputs to the symbol encoder 11 which encodes the frame symbols into amplitude and phase coded symbols 12 which could be complex $\{Z(u)\}$ or real $\{R(u_R), I(u_I)\}$ depending on the application. These symbols 12 are the inputs to the current real Walsh CDMA encoding in equations (1). Inputs $\{Z(u)\}$, $\{R(u_R)$, 12 are real Walsh encoded, summed over the users, scrambled by PN in the current real Walsh CDMA encoder 13 generate the complex output chips {Z(n)} 14. This encoding 13 is a representative implementation of equations (1). These output chips Z(n) are waveform modulated 15 to generate the analog complex signal z(t) which is single sideband upconverted, amplified, and transmitted (Tx) by the analog front end of the 15 as the real waveform v(t) 16 at the carrier transmitter frequency f_0 whose amplitude is the real part of the complex envelope of the baseband waveform z(t) multiplied by the carrier frequency and the phase angle ϕ accounts for the phase change from the baseband signal to the transmitted signal.

It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 1 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

FIG. 2 real Walsh CDMA encoding is a representative implementation of the real Walsh CDMA encoding 13 in FIG. 1 and in equations (1). Inputs are the user data symbols which could be complex $\{Z(u)\}$ or real $\{R(u_R) + jI(u_I)\}$ 17. For complex and real data symbols the encoding of each user by the corresponding Walsh code is described in 18 by the implementation of transferring the sign of each Walsh code chip to the user data

symbol followed by a 1-to-N expander 1¹N of each data symbol into an N chip sequence using the sign transfer of the Walsh chips.

For complex data symbols {Z(u)} the sign-expander operation generates the N-chip sequence $Z(u,n) = Z(u) sgn\{W(u,n)\} =$ Z(u) W(u,n) for n=0,1,...,N-1 for each user u=0,1,...,N-1. Walsh encoding serves to spread each user data symbol into an orthogonally encoded chip sequence which is spread over the CDMA communications frequency band. The Walsh encoded chip sequences for each of the user data symbols are summed over the users with the scrambling PN encoding followed by PN encoding is implemented by transferring 21. $[P_R(n)+jP_I(n)]$ the sign of each PN chip to the summed chip of the Walsh encoded data symbols. Output is the stream of complex CDMA encoded chips 20 selects the appropriate signal 22. The switch $\{Z(n)\}$ processing path for the complex and real data symbols.

For real data symbols $\{R(u_R)+jI(u_I)\}$ the real and imaginary communications axis data symbols are separately Walsh encoded 18, summed 19, and then PN encoded 19 to provide orthogonality between the channels along the real and imaginary communications axes. Output is complex combined 19 and PN encoded with the scrambling sequence $[P_R(n)+jP_I(n)]$ 21. Output is the stream of complex CDMA encoded chips $\{Z(n)\}$ 22.

It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 2 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

FIG. 3 CDMA receiver block diagram is representative of a current CDMA receiver which includes an implementation of the current real Walsh CDMA decoding in equations (2). This block diagram becomes a representative implementation of the CDMA receiver which implements the new complex Walsh CDMA decoding when the current real Walsh CDMA decoding 27 is replaced by

the new complex Walsh CDMA decoding of this invention. FIG. 3 signal processing starts with the user transmitted wavefronts incident at the receiver antenna 23 for the n_u users $u=1,..., n_u \le$ These wavefronts are combined by addition in the antenna to form the receive (Rx) signal $\hat{v}(t)$ at the antenna output 23 where $\hat{v}(t)$ is an estimate of the transmitted signal v(t) 16 in FIG. 1, that is received with errors in time Δ t, frequency Δ f, phase $\Delta\theta$, and with an estimate $\hat{z}(t)$ of the transmitted complex baseband This received signal $\hat{v}(t)$ is **16** in FIG. 1. signal z(t) amplified and downconverted by the analog front end 24 and then synchronized and analog-to-digital (ADC) converted from the ADC are filtered and chip detected 26 by the fullband chip detector, to recover estimates $\{\hat{Z}(n) = \hat{R}(n) + j\hat{I}(n)\}\}$ 28 the transmitted signal which is the stream of complex CDMA encoded chips $\{Z(n)=R(n)+jI(n)\}$ 14 in FIG. 1 for both complex and real data symbols. The CDMA decoder 27 implements the algorithms in equations (2) by stripping off the PN code(s) and decoding the received CDMA real Walsh orthogonally encoded chips to recover estimates $\{\hat{Z}(u) = \hat{R}(u_n) + i\hat{I}(u_n)\}$ 29 of the transmitted $\{Z(u) = R(u_R) + jI(u_I)\}$ 12 in FIG. 1. user data symbols Notation introduced in FIG. 1 and 3 assumes that the user index $u=u_R=u_I$ for complex data symbols, and for real data symbols the user index u is used for counting the user pairs (u_R, u_I) of real These estimates are processed by the and complex data symbols. and the frame processor 31 to recover symbol decoder 30 32 of the transmitted user data words. estimates

It should be obvious to anyone skilled in the communications art that this example implementation clearly defines the fundamental current CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

FIG. 4 real Walsh CDMA decoding is a representative implementation of the real Walsh CDMA decoding 27 in FIG. 3 and in equations (2). Inputs are the received estimates of the complex CDMA encoded chips $\{\hat{Z}(n)\}$ 33. The PN scrambling code is stripped off from these chips 34 by changing the sign of each chip according to the numerical sign of the real and imaginary components of the complex conjugate of the PN code as per the decoding algorithms 8 in equations (2).

For complex data symbols 35 the real Walsh channelization coding is removed by a pulse compression operation consisting of multiplying each received chip by the numerical sign of the corresponding Walsh chip for the user and summing the products over the N Walsh chips 36 to recover estimates $\{\hat{Z}(u)\}$ of the user complex data symbols $\{Z(u)\}$. The switch 35 selects the appropriate signal processing path for the complex and real data symbols.

For real data symbols 35 the next signal processing operation is the removal of the PN codes from the real and imaginary axes. This is followed by stripping off the real Walsh channelization coding by multiplying each received chip by the numerical sign of the corresponding Walsh chip for the user and summing the products over the N Walsh chips 36 to recover estimates $\{\hat{R}(u_R), \hat{I}(u_I)\}$ of the user real data symbols $\{R(u_R), I(u_I)\}$.

It should be obvious to anyone skilled in the communications art that this example implementation clearly defines the fundamental current CDMA signal processing relevant

to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

For cellular applications the transmitter description describes the transmission signal processing applicable to this invention for both the hub and user terminals, and the receiver describes the corresponding receiving signal processing for the hub and user terminals for applicability to this invention.

SUMMARY OF INVENTION

This invention is a new approach to the application of Walsh orthogonal codes for CDMA, which replaces the current real Walsh codes with the new complex Walsh codes and the hybrid complex Walsh codes disclosed in this invention. Real Walsh codes are used for current CDMA applications and will be used for all of the future CDMA systems. This invention of complex Walsh codes will provide the choice of using the new complex Walsh codes or the real Walsh codes since the real Walsh codes are the real components of the complex Walsh codes. This means an application capable of using the complex Walsh codes can simply turn-off the complex axis components of the complex Walsh codes for real Walsh CDMA coding and decoding.

The complex Walsh codes of this invention are proven to be the natural development for the Walsh codes and therefore are the correct complex Walsh codes to within arbitrary factors that include scale and rotation, which are not relevant to performance. This natural development of the complex Walsh codes in the N-dimensional complex code space C^N extended the correspondences between the real Walsh codes and the Fourier N-dimensional real code space R^N . codes in the correspondences between the complex Walsh codes and the discrete Fourier transform (DFT) codes in CN.

The new 4-phase complex Walsh orthogonal CDMA codes provide fundamental performance improvements compared to the 2-phase real Walsh codes which include an increase in the carrier-to-noise

ratio (CNR) for data symbol recovery in the receiver, lower correlation side-lobes under timing offsets both with and without PN spreading, lower levels of harmonic interference caused by non-linear amplification of multi-carrier CDMA signals, and reduced phase tracking jitter for code tracking to support both acquisition and synchronization. These potential performace improvements simply reflect the widely known principle that complex CDMA is better than real CDMA.

The new hybrid complex Walsh orthogonal CDMA codes increase the choices for the code length by allowing the combined use of complex Walsh and discrete Fourier transform complex orthogonal codes using a Kronecker construction, direct sum construction, as well as the possibility for more general functional combining.

BRIEF DESCRIPTION OF DRAWINGS AND PERFORMACE DATA

The above-mentioned and other features, objects, design algorithms, and performance advantages of the present invention will become more apparent from the detailed description set forth below when taken in conjunction with the drawings and performance data wherein like reference characters and numerals denote like elements, and in which:

- FIG. 1 is a representative CDMA transmitter signal processing implementation block diagram, with emphasis on the current real Walsh CDMA encoding which contains the signal processing elements addressed by this invention disclosure.
- FIG. 2 is a representative CDMA encoding signal processing implementation diagram, with emphasis on the current real Walsh CDMA encoding which contains the signal processing elements addressed by this invention disclosure.
- FIG.3 is a representative CDMA receiver signal processing implementation block diagram, with emphasis on the current real Walsh CDMA decoding which contains the signal processing elements addressed by this invention disclosure.
- FIG. 4 is a representative CDMA decoding signal processing implementation diagram, with emphasis on the current real Walsh

CDMA decoding which contains the signal processing elements addressed by this invention disclosure.

FIG.5 is a representative correlation plot of the correlation between the complex discrete Fourier transform (DFT) cosine and sine code component vectors and the real Fourier transform cosine and sine code component vectors.

FIG.6 is a representative CDMA encoding signal processing implementation diagram, with emphasis on the new complex Walsh CDMA encoding which contains the signal processing elements addressed by this invention disclosure

FIG.7 is a representative CDMA decoding signal processing implementation diagram, with emphasis on the new complex Walsh CDMA decoding which contains the signal processing elements addressed by this invention disclosure.

DISCLOSURE OF INVENTION

Real orthogonal CDMA code space R^N for Hadamard, Walsh, and The new complex Walsh orthogonal CDMA codes are derived from the current real Walsh codes by starting with the correspondence of the current real Walsh codes with the discrete (DFT) basis vectors. Consider the real Fourier transform orthogonal CDMA code space RN consisting of N-orthogonal real code vectors. Examples of code sets in R^N include the Hadamard, Walsh, and Fourier. The corresponding matrices of code vectors are designated as H, W, F respectively and as defined in equations (1) respectively consist of N-rows of N-chip code vectors. Hadamard codes in their reordered form known as Walsh codes are used in the current CDMA, in the proposals for the next generation G3 CDMA, and in the proposals for all future CDMA. Walsh codes reorder the Hadamard codes according to increasing sequency. These codes assumed +/-1 values. Sequency is the average rate of change of the sign of the codes and the

reordering places the Walsh codes in correspondence to the DFT wherein sequency is in correspondence with frequency in the DFT.

It is important to note that the correspondence "sequency" frequency" only applies to the complex DFT matrix E consisting of the N-row vectors $\{E(u) = [E(u,0),...,E(u,N-1)]\}$ wherein the elements of E are $E(u,n) = e^{i(2\pi u n/N)}$, $u,n=0,1,...,N-1\}$. Historically it has not been applied to the Fourier basis F in \mathbb{R}^N .

(1) define the three sets H,W,F of real Equations orthogonal codes in R^{N} with the understanding that the H and W are identical except for the ordering of the code vectors. orthogonal functions are basis Hadamard 37 and Walsh 38 vectors in RN and are used as code vectors for orthogonal CDMA channelization coding. Hadamard 37 and Walsh 38 equations of definition are widely known with examples given in Reference [6]. 39 equations of definition are widely Likewise, the Fourier known within the engineering and scientific communities, wherein

N-chip real orthogonal CDMA codes

(3)

37 Hadamard codes

- H = Hadamard NxN orthogonal code matrix consisting of N rows of N chip code vectors
 - = [H(u)] matrix of row vectors H(u)
 - = [H(u,n)] matrix of elements H(u,n)
- H(u) = Hadamard code vector u
 - = [H(u,0), H(u,1), ..., H(u,N-1)]
 - = 1xN row vector of chips H(u,0),...,H(u,N-1)
- H(u,n) = Hadamard code u chip n
 - = +/+1 possible values

$$= (-1) \quad \begin{bmatrix} i=M-1 \\ \sum_{i=0}^{n} u_i n_i \end{bmatrix}$$

where $u = \sum_{i=0}^{i=M-1} u_i 2^i$ binary representation of u

$$n = \sum_{i=0}^{i=M-1} n_i 2^i \text{ binary representation of } n$$

38 Walsh codes

W = Walsh NxN orthogonal code matrix consisting of N rows of N chip code vectors

= [W(u)] matrix of row vectors W(u)

= [W(u,n)] matrix of elements W(u,n)

W(u) =Walsh code vector u

=
$$[W(u,0), W(u,1), ..., W(u,N-1)]$$

W(u,n) = Walsh code u chip n

= +/+1 possible values

$$= (-1)^{n} \left[u_{M-1}^{n_0} + \sum_{i=1}^{i=M-1} (u_{M-1-i} + u_{M-i})^{n_i} \right]$$

39 Fourier codes

F = Fourier NxN orthogonal code matrix consisting of

N rows of N chip code vectors

=
$$[F(u)]$$
 matrix of row vectors $F(u)$

$$=$$
 $\left[\frac{C}{S}\right]$

 $C = N/2+1 \times N \text{ matrix of row vectors } C(u)$

C(u) = Even code vectors for u=0,1,...,N/2

= $[1, \cos(2\pi u1/N), ..., \cos(2\pi u(N-1/N))]$

 $S = N/2-1 \times N \text{ matrix of row vectors } S(u)$

 $S(\Delta u) = Odd code vectors for <math>u=N/2+\Delta u$, $\Delta u=1,2,...,N/2-1$

= $[\sin(2\pi \Delta u 1/N),...,\sin(2\pi \Delta u(N-1)/N)]$

where
$$F(u) = C(u)$$
 for $u=0,1,...,N/2$

=
$$S(\Delta u)$$
 for $\Delta u = u-N/2$, $u=N/2+1$,..., $N-1$

the cosine C(u) and sine S(u) code vectors are the code vectors of the Fourier code matrix F.

Complex orthogonal CDMA code space C^N for DFT codes: The DFT orthogonal codes are a complex basis for the complex N-dimensional CDMA code space C^N and consist of the DFT harmonic code vectors arranged in increasing order of frequency. Equations (4) are the definition of the DFT code vectors. The DFT definition 40 is widely known within the engineering and scientific communities. Even and odd components of the DFT code

vectors 41 are the real cosine code vectors $\{C(u)\}$ and the imaginary sine code vectors $\{S(u)\}$ where even and odd are referenced to the midpoint of the code vectors. These cosine and sine code vectors are the extended set 2N of the N Fourier cosine and sine code vectors.

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(4)
N-chip DFT complex orthogonal CDMA codes
40 DFT code vectors
        = DFT NxN orthogonal code matrix consisting of
   E
            N rows of N chip code vectors
         = [ E(u) ] matrix of row vectors E(u)
         = [E(u,n)] matrix of elements E(u,n)
        = DFT code vector u
  E(u)
          = [E(u,0), E(u,1), ..., E(u,N-1)]
          = 1xN row vector of chips E(u, 0), ..., E(u, N-1)
  E(u,n) = DFT \text{ code } u \text{ chip } n
          = e^{j2\pi un/N}
          = cos(2\pi un/N) + jsin(2\pi un/N)
           = N possible values on the unit circle
41 Even and odd code vectors are the extended set of
    Fourier even and odd code vectors in 39 equations (3_)
    C(u) = Even code vectors for u=0,1,...,N-1
         = [1, \cos(2\pi u 1/N), ..., \cos(2\pi u (N-1)/N)]
    S(u) = Odd code vectors for u=0,1,...,N-1
```

Complex orthogonal CDMA code space C^N for complex Walsh codes: Step 1 in the derivation of the complex Walsh codes in this invention establishes the correspondence of the even and odd Walsh codes with the even and odd Fourier codes. Even and odd for these codes are with respect to the midpoint of the row vectors similar to the definition for the DFT vector codes 41 in equations (4). Equations (5) identify the even and odd Walsh codes in the W basis in R^N. These even and odd Walsh codes can be placed in

E(u) = C(u) + j S(u)

= $[0, \sin(2\pi u 1/N), ..., \sin(2\pi u (N-1)/N)]$

for u=0,1,...,N-1

. Even and odd Walsh codes in R^N

(5)

 $W_e(u)$ = Even Walsh code vector

= W(2u) for u=0,1,...,N/2-1

 $W_o(u)$ = Odd Walsh code vectors

= W(2u-1) for u=1,...,N/2

direct correspondence with the Fourier code vectors **39** in equations (3) using the DFT equations (4). This correspondence is defined in equations (6) where the correspondence operator "~" represents the even and odd correspondence between the Walsh and Fourier codes, and additionally represents the sequency~frequency correspondence.

Correspondence between Walsh and Fourier codes (6)

 $W(0) \sim C(0)$

 $W_e(u) \sim C(u)$ for u=1,...,N/2-1

 $W_o(u) \sim S(u)$ for u=1,...,N/2-1

 $W(N-1) \sim C(N/2)$

Step 2 derives the set of N complex DFT vector codes in C^N from the set of N real Fourier vector codes in R^N . This means that the set of 2N cosine and sine code vectors in **41** in equations (4) for the DFT codes in C^N will be derived from the set of N cosine and sine code vectors in **39** in equations (3) for the Fourier codes in R^N . The first N/2+1 code vectors of the DFT basis can be written in terms of the Fourier code vectors in equations (7).

DFT code vectors 0,1,...,N/2 derived from Fourier (7)

- 42 Fourier code vectors from 39 in equations (3) are
 - C(u) = Even code vectors for u=0,1,...,N/2
 - = $[1, \cos(2\pi u1/N), ..., \cos(2\pi u(N-1/N))]$
 - S(u) = Odd code vectors for u=1,2,...,N/2-1
 - = $[\sin(2\pi u1/N),...,\sin(2\pi u(N-1)/N)]$
- 43 DFT code vectors in 41 of equations (4) are written as functions of the Fourier code vectors
 - E(u) = DFT complex code vectors for u=0,1,...,N/2= C(0)

=
$$C(u)+jS(u)$$
 for $u=1,...,N/2-1$
= $C(N/2)$ for $u=N/2$

The remaining set of N/2+1,...,N-1 DFT code vectors in C^N can be derived from the original set of Fourier code vectors by a correlation which establishes the mapping of the DFT codes onto the Fourier codes. We derive this mapping by correlating the real and imaginary components of the DFT code vectors with the corresponding even and odd components of the Fourier code vectors. The correlation operation is defined in equations (8)

Correlation of DFT and Fourier code vectors (8)

Corr(even) = C Real(E')

- = Correlation matrix
- = Matrix product of C and the real part
 of E transpose

Corr(odd) = S Imag{E'}

- = Correlation matrix
- = Matrix product of S and the imaginary
 part of E transpose

and the results of the correlation calculations are plotted in FIG.5 for N=32 for the real cosine and the odd sine Fourier code vectors. Plotted are the correlation of the 2N DFT cosine and sine codes against the N Fourier cosine and sine codes which range from -15 to +16 where the negative indices of the codes represent a negative correlation value. The plotted curves are the correlation peaks. These correlation curves in FIG. 5 prove that the remaining N/2+1,...,N-1 code vectors of the DFT are derived from the Fourier code vectors by equations (9)

$$E(u) = C(N/2 - \Delta u) - jS(N/2 - \Delta u)$$
for $u = N/2 + \Delta u$

$$\Delta u = 1, ..., N/2 - 1$$

This construction of the remaining DFT basis in equations (9) is an application of the DFT spectral foldover property which

observes the DFT harmonic vectors for frequencies $fNT=N/2+\Delta i$ above the Nyquist sampling rate fNT=N/2 simply foldover such that the DFT harmonic vector for $fNT=N/2+\Delta i$ is the DFT basis vector for $fNT=N/2-\Delta i$ to within a fixed sign and fixed phase angle of rotation.

Step 3 derives the complex Walsh code vectors from the real Walsh code vectors by using the DFT derivation in equations (7) and (9), by using the correspondences between the real Walsh and Fourier in equations (6), and by using the fundamental correspondence between the complex Walsh and the complex DFT given in equation (10). We start by constructing the complex

Correspondence between complex Walsh and DFT (10)

 \widetilde{W} ~ E NxN complex DFT orthogonal code matrix where \widetilde{W} = NxN complex Walsh orthogonal code matrix = N rows of N chip code vectors = [\widetilde{W} (u)] matrix of row vectors \widetilde{W} (u) = [\widetilde{W} (u,n)] matrix of elements \widetilde{W} (u,n) \widetilde{W} (u) = Complex Walsh code vector u = [\widetilde{W} (u,0), \widetilde{W} (u,1), ..., \widetilde{W} (u,N-1)] \widetilde{W} = +/-1 +/- j possible value

Walsh dc code vector \widetilde{W} (0). We use equation E(0)=C(0) in 43 in equations (7), the correspondence in equations (6), and observe that the dc complex Walsh vector has both real and imaginary components in the \widetilde{W} domain, to derive the dc complex Walsh code vector:

$$\widetilde{W}$$
 (0) = W(0) + jW(0) for u=0 (11)

For complex Walsh code vectors $\widetilde{W}(u)$, u=1,2,...,N/2-1, we apply the correspondences in equations (10) between the complex Walsh and DFT bases, to the DFT equations **43** in equations (7):

$$\widetilde{W}(u) = W_e(u) + jW_o(u)$$
 for u=1,2,...,N/2-1 (12)
= W(2u) + jW(2u-1) for u=1,2,...,N/2-1

For complex Walsh code vector $\widetilde{W}(N/2)$ we use the equation E(N/2)=C(N/2) in equations (7) and the same rationale used to derive equation (11), to yield the equation for $\widetilde{W}(N/2)$.

$$\widetilde{W}(N/2) = W(N-1) + jW(N-1)$$
 for $u=N/2$ (13)

For complex Walsh code vectors $\widetilde{W}(N/2+\Delta u)$, $\Delta u=1,2,...,N/2-1$ we apply the correspondences between the complex Walsh and DFT bases to the spectral foldover equation $E(N/2+\Delta u)=C(N/2-\Delta u)-jS(N/2-\Delta u)$ in equations (9) with the changes in indexing required to account for the W indexing in equations (5). The equations are

$$\widetilde{W}(N/2 + \Delta u) = W(N-1-\Delta eu) + W(N-1-\Delta ou)$$
 for $u=N/2+1,...,N-1$ (14)
= $W(N-1-2\Delta u) + jW(N-2\Delta u)$ for $u=N/2+1,...,N-1$

using the notation $\Delta ei=2\Delta i$, $\Delta oi=2\Delta i-1$. These complex Walsh code vectors in equations (11), (12), (13), (14) are the equations of definition for the complex Walsh code vectors.

An equivalent way to derive the complex Walsh code vectors in C^N from the real Walsh basis in R^{2N} is to use a sampling technique which is a known method for deriving a complex basis in C^N from a real basis in R^N .

Transmitter equations (15) describe a representative complex Walsh CDMA encoding for the transmitter in FIG. 1. It is assumed that there are N complex Walsh code vectors $\widetilde{W}(u)$ 44 each of length N chips similar to the definitions for the real Walsh code vectors 1 in equations (1). The code vector is presented by a 1xN N-chip row vector $\widetilde{W}(u) = [\widetilde{W}(u,0),...,\widetilde{W}(u,N-1)]$ where $\widetilde{W}(u,n)$ is chip n of code u. The code vectors are the row vectors of the complex Walsh matrix \widetilde{W} . Walsh code chip n of code vector u has the possible values $\widetilde{W}(u,n) = +/-1 +/-j$. Each user is assigned a unique Walsh code which allows the code vectors to be designated by the user symbols u=0,1,...,N-1 for N complex Walsh codes. The complex Walsh code vectors $\widetilde{W}(u)$ derived

in equations (11),(12),(13),(14) are summarized 44 in terms of their real and imaginary component code vectors $\widetilde{W}(u) = W_R(u) + jW_I(u)$ where $W_R(u)$ and $W_I(u)$ are respectively the real and imaginary component code vectors. As per the derivation of $\widetilde{W}(u)$ the sets of real axis code vectors $\{W_R(u)\}$ and the imaginary axis code vectors $\{W_I(u)\}$ both consist of the real Walsh code vectors in \mathbb{R}^N with the ordering modified to ensure that the definition of the complex Walsh vectors satisfies equations (11), (12), (13), (14).

Complex Walsh CDMA encoding for transmitter (15)

- 44 Complex Walsh codes use the definitions for the real Walsh codes in 1 equations (1) and the definitions of the complex Walsh codes in equations (11), (12), (13), (14). We find
 - \widetilde{W} = complex Walsh NxN orthogonal code matrix consisting of N rows of N chip code vectors
 - = [\widetilde{W} (u)] matrix of row vectors \widetilde{W} (u)
 - = $[\widetilde{W}(u,n)]$ matrix of elements $\widetilde{W}(u,n)$
 - \widetilde{W} (u) = complex Walsh code vector u
 - = $W_R(u) + jW_I(u)$ for u=0,1,...,N-1

where

$$W_{R}(u) = \text{Real} \{ \widetilde{W}(u) \}$$
 $= W(0)$ for $u=0$
 $= W(2u)$ for $u=1,2,...,N/2-1$
 $= W(N-1)$ for $u=N/2$
 $= W(2N-2u-1)$ for $u=N/2+1,...,N-1$
 $W_{I}(u) = \text{Imag} \{ \widetilde{W}(u) \}$
 $= W(0)$ for $u=0$
 $= W(2u-1)$ for $u=1,2,...,N/2-1$
 $= W(N-1)$ for $u=N/2$
 $= W(2N-2u)$ for $u=N/2+1,...,N-1$

$$\widetilde{W}$$
 (u,n) = complex Walsh code u chip n
= +/-1 +/-j possible values

45 Data symbols

$$Z(u)$$
 = Complex data symbol for user u
= $R(u) + jI(u)$

46 Complex Walsh encoded data

$$\begin{split} Z(u,n) &= Z(u) \ \widetilde{W}(u,n) \\ &= Z(u) \left[sgn\{W_R(u,n)\} + jsgn\{W_I(u,n)\} \right] \\ &= \left[R(u) sgn\{W_R(u,n)\} - I(u) sgn\{W_I(u,n)\} \right] \\ &+ j \left[R(u) sgn\{W_I(u,n) + I(u,n) sgn\{W_R(u,n)\} \right] \end{split}$$

47 PN scrambling

 $P_R(n)$ = Chip n of the PN code for the real axis

 $P_{I}(n)$ = Chip n of the PN code for the imaginary axis

Z(n) = PN scrambled complex Walsh encoded data chips
after summing over the users

$$= \sum_{u} Z(u,n) [P_{R}(n) + j P_{I}(n)]$$

$$= \sum_{n} Z(u,n) \left[\operatorname{sgn} \{ P_{R}(n) \} + j \operatorname{sgn} \{ P_{I}(n) \} \right]$$

= Complex Walsh CDMA encoded chips

User data symbols 45 are the set of complex symbols $\{Z(u), u=0,1...,N-1\}$. These data symbols are encoded by the Walsh CDMA codes 46. Each of the user symbols Z(u) is assigned a unique complex Walsh code $\widetilde{W}(u)=W_R(u)+jW_I(u)$. Complex Walsh encoding of each user data symbol generates an N-chip sequence with each chip in the sequence consisting of the user data symbol with the complex sign of the corresponding complex Walsh code chip, which means each encoded chip = [Data symbol Z(u)] x [Sign of $W_R(u)$ + j sign of $W_I(u)$].

The complex Walsh encoded data symbols are summed and encoded with PN scrambling codes 47. These PN codes are defined 4 in equations (1) as a complex PN for each chip n, equal to $[P_R(u) + j P_I(u)]$ where $P_R(u)$ and $P_I(u)$ are the respective PN

scrambling codes for the real and imaginary axes. Encoding with the complex PN is the same as given $\bf 4$ in equations (1) for complex data symbols. Each complex Walsh encoded data chip Z(u,n) $\bf 46$ is summed over the set of users u=0,1,...,N-1 and complex PN encoded to yield the complex Walsh CDMA chips Z(n) = $\sum Z(u,n) \left[P_R(n) + j P_I(n) \right] \bf 47$.

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA encoding in equations (1) since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

Receiver equations (16) describe a representative complex Walsh CDMA decoding for the receiver in FIG. 3. The receiver $\{\hat{Z}(n)\}$ front end 48 provides estimates of the transmitted complex Walsh CDMA encoded chips {Z(n)} for the complex data symbols {Z(u)}. Orthogonality property 49 is expressed as a matrix product of the complex Walsh code chips or equivalently as a matrix produce of the complex Walsh code chip numerical signs of the real and imaginary components. The 2-phase PN codes 50 have the useful decoding property that the square of each code chip is unity which is equivalent to observing that the square of each code chip numerical sign is unity. Decoding algorithms 51 perform the inverse of the signal processing for the encoding in equations (15) to recover estimates $\{\hat{Z}(u)\}$ of the transmitter user symbols $\{Z(n)\}\$ for the complex data symbols $\{Z(u)\}\$.

Complex Walsh CDMA decoding for receiver (16)

- 48 Receiver front end in FIG. 3 provides estimates $\{\hat{Z}(n)\}$ 28 of the encoded transmitter chip symbols $\{Z(n)\}$ 47 in equations (15).
- **49** Orthogoality property of complex Walsh NxN matrix \widetilde{W}

$$\begin{split} \sum_{n} \widetilde{W}(\hat{u}, n) \, \widetilde{W}^*(n, u) &= \\ \sum_{n} \left[\operatorname{sgn} \left\{ W_{R}(\hat{u}, n) \right\} + j \operatorname{sgn} \left\{ W_{I}(\hat{u}, n) \right\} \right] \left[\operatorname{sgn} \left\{ W_{R}(n, u) - j \operatorname{sgn} \left\{ W_{I}(n, u) \right\} \right] \right] \\ &= 2 \operatorname{N} \ \delta(\hat{u}, u) \\ &= \operatorname{Delta} \ \text{function of} \ \hat{u} \text{ and } u \\ &= 1 \quad \text{for} \quad \hat{u} = u \\ &= 0 \quad \text{otherwise} \end{split}$$

50 PN decoding property

$$P(n) P(n) = sgn\{P(n)\} sgn\{P(n)\}$$

= 1

51 Decoding algorithm

$$\hat{Z}(u) = 2^{-1}N^{-1}\sum_{n}\hat{Z}(n)\left[sgn\{P_{R}(n)\}-j\,sgn\{P_{I}(n)\}\right]\left[sgn\{W_{R}(n,u)\}-j\,sgn\{W_{I}(n,u)\}\right]$$

$$= \text{Receiver estimate of the transmitted data symbol}$$

$$Z(u) \quad \textbf{45} \quad \text{in equations (15)}$$

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA decoding in FIG. 4 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

FIG. 6 complex Walsh CDMA encoding is a representative implementation of the complex Walsh CDMA encoding which will replace the current real Walsh encoding 13 in FIG. 1, and defined in equations (15). Inputs are the user data symbols {Z(u)} 52. Encoding of each user by the corresponding complex Walsh code is described in 53 by the implementation of transferring the sign +/-1+/-j of each complex Walsh code chip to the user data symbol followed by a 1-to-N expander 11N of each data symbol into an N chip sequence using the sign transfer of the complex Walsh chips.

The sign-expander operation 53 generates the N-chip sequence $Z(u,n)=Z(u)\left[sgn\{W_R(u,n)\}+jsgn\{W_I(u,n)\}\right]=$

 $Z(u)[W_R(u,n)+jW_I(u,n)]$ for n=0,1,...,N-1 for each user u=0,1,...,N-This complex Walsh encoding serves to spread each user data symbol into an orthogonally encoded chip sequence which is spread over the CDMA communications frequency band. The complex Walsh encoded chip sequences for each of the user data symbols are summed over the users 54 followed by PN encoding with the scrambling sequence $[P_R(n)-jP_I(n)]$ **55**. PN encoding is implemented by transferring the sign of each PN chip to the summed chip of the Walsh encoded data symbols. Output is the stream of complex CDMA encoded chips {Z(n)} 56.

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA encoding in FIG. 2 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 6 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

FIG. 7 complex Walsh CDMA decoding is a representative implementation of complex Walsh CDMA decoding which will replace the current real Walsh decoding 27 in FIG. 3, and defined in equations (15). Inputs are the received estimates of the complex CDMA encoded chips $\{\hat{Z}(n)\}$ 57. The PN scrambling code is stripped off from these chips 58 by changing the sign of each chip according to the numerical sign of the real and imaginary components of the complex conjugate of the PN code as per the decoding algorithms 50 in equations (16).

The complex Walsh channelization coding is removed by a pulse compression operation consisting of multiplying each received chip by the numerical sign of the corresponding complex

Walsh chip for the user and summing the products over the N Walsh chips ${\bf 59}$ to recover estimates $\{\hat{Z}(u)\}$ of the user complex data symbols $\{{\bf Z}(u)\}$.

Although not considered in this example, it is possible to use combinations of both complex and real data symbols similar to the approach for real Walsh CDMA decoding in FIG. 4 since the complex Walsh code vectors are the real Walsh code vectors along the real axis and a reordering of the real Walsh code vectors along the imaginary axis.

It should be obvious to anyone skilled in the communications art that this example implementation in FIG. 6 clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches.

For cellular applications the transmitter description describes the transmission signal processing applicable to this invention for both the hub and user terminals, and the receiver describes the corresponding receiving signal processing for the hub and user terminals for applicability to this invention.

Complex orthogonal CDMA code space C^N for hybrid complex Walsh codes: The power of 2 code lengths $N=2^N$ where M is an integer, for complex Walsh can be modified to allow the code length N to be a product of powers of primes 60 in equations (17) or a sum of powers of primes 61 in equations (17), at the implementation cost of introducing multiply operations into the CDMA encoding and decoding. In the previous disclosure of this invention we used N equal to a power of 2 which means $N=2^m$ corresponding to $p_0=2$ and $M=m_0$. This restriction was made for convenience in explaining the construction of the complex Walsh and is not required since it is well known that Hadamard matrices exist for non-integer powers of 2 and, therefore, complex Walsh matrices exist for non-integer powers of 2.

Length N of hybrid complex Walsh orthogonal codes (17)

60 Kronecker product code construction

$$N = \prod_{k} p_k^{m_k}$$
$$= \prod_{k} N_k$$

where

 P_k = prime number indexed by k starting with k=0

 m_k = order of the prime number p_k

 N_k = Length of code for the prime p_k

$$= p_k^{m_k}$$

61 Direct sum code construction

$$N = \sum_{k} p_k^{m_k}$$
$$= \sum_{k} N_k$$

Add-only arithemetic operations are required for encoding and decoding both real Walsh and complex Walsh CDMA codes since the real Walsh values are +/-1 and the complex Walsh values are +/-1 +/-j which means the only operations are sign transfer and adds plus subtracts or add-only. Multiply operations are more complex to implement than add operations. However, the of having greater flexibility in choosing the advantages orthogonal CDMA code lengths N'using equations (17) can offset the expense of multiply operations for particular applications. Accordingly, this invention includes the concept of hybrid complex Walsh orthogonal CDMA codes with the flexibility to meet This extended class of complex Walsh codes are hybrid in that their construction supplements the complex Walsh codes with the use of Hadamard (or real Walsh), DFT, and other orthogonal codes.

Hybrid complex Walsh orthogonal CDMA codes can be constructed as demonstrated in 64 and 65 in equations (18) for the Kronecker product, and in 66 in equations (18) for the direct sum. Code matrices considered 62 in equations (18)

for the construction of the hybrid complex Walsh are the DFT E and Hadamard H, in addition to the complex Walsh \widetilde{W} . algorithms and examples for the construction start with the of the NxN orthogonal code matrices \widetilde{W}_{N} , E_{N} , H_{N} definitions 63 for \widetilde{W} ,E,H respectively, examples for low orders N=2,4, and the equivalence of E4 and \widetilde{W}_4 after the \widetilde{W}_4 is rotated through the -90 degrees and rescaled. The CDMA current and developing standards use the prime 2 which generates a code length N=2^M where M=integer. For applications requiring greater flexibility in code length N, additional primes can used using the Kronecker construction. We illustrate this in 65 with the addition of prime=3. The use of prime=3 in addition to the prime=2 in the range of N=8 to 64 is observed to increase the number of N choices from 4 to 9 at a modest cost penality of using multiples of the angle increment 30 degrees for prime=3 in addition to the angle increment 90 degrees for prime=2. As noted in there are several choices in the ordering of the Kronecker product construction and 2 of these choices are used in the construction.

Direct sum construction provides greater flexibility in the choice of N without necessarily introducing a multiply penality. However, the addition of the zero matrix in the construction is generally not desirable for CDMA communications.

Construction of hybrid complex Walsh orthogonal codes (18)

62 Code matrices

 $\widetilde{W}_{\scriptscriptstyle N}$ = NxN complex Walsh orthogonal code matrix

 E_N = NxN DFT orthogonal code matrix

 H_N = NxN Hadamard orthogonal code matrix

63 Low-order code definitions and equivalences

$$2x2 \qquad H_2 \qquad = \left[\begin{array}{cc} 1 & 1 \\ 1 & -1 \end{array} \right]$$

 $= E_2$

$$= (e^{-j\pi/4}/\sqrt{2}) \star \widetilde{W}_2$$

$$\widetilde{W_4} = \begin{bmatrix} 1+j & 1+j & 1+j & 1+j \\ 1+j & -1+j & -1-j & 1-j \\ 1+j & -1-j & 1+j & -1-j \\ 1+j & 1-j & -1-j & -1+j \end{bmatrix}$$

$$E_4 = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & j & -1 & -j \\ 1 & -1 & 1 & -1 \\ 1 & -j & -1 & j \end{bmatrix}$$

$$= (e^{-j\pi/4}/\sqrt{2}) \widetilde{W}_4$$

64 Kronecker product construction for $N = \prod_k N_k$ Code matrix $C_N = NxN$ hybrid orthogonal CDMA code matrix Kronecker product construction of C_N

$$C_N = C_0 \prod_{k>0} \bigotimes C_{N_k}$$

Kronecker product definition

 $A = N_a x N_a$ orthogonal code matrix

 $B = N_b x N_b orthogonal code matrix$

 $A \otimes B$ = Kronecker product of matrix A and matrix B

- = $N_a N_b \times N_a N_b$ orthogonal code matrix consisting of the elements $[a_{ik}]$ of matrix A multiplied by the matrix B
- $= [a_{ik} B]$
- 65 Kronecker product construction examples for primes p=2,3 and the range of sizes $8 \le N \le 64$

$$8x8$$
 $C_8 = \widetilde{W}_8$

$$12x12 \quad C_{12} = \widetilde{W}_4 \otimes E_3$$

$$C_{12} = E_3 \otimes \widetilde{W}_4$$

$$16x16 \quad C_{16} = \widetilde{W}_{16}$$

$$18 \times 18 \quad C_{18} = \widetilde{W}_2 \otimes E_3 \otimes E_3$$

$$C_{18} = E_3 \otimes E_3 \otimes \widetilde{W}_2$$

$$24 \times 24 \quad C_{24} = \widetilde{W}_8 \otimes E_3$$

$$C_{24} = E_3 \otimes \widetilde{W}_8$$

$$32 \times 32 \quad C_{32} = \widetilde{W}_{32}$$

$$36 \times 36$$
 $C_{36} = \widetilde{W}_4 \otimes \widetilde{W}_3 \otimes \widetilde{W}_3$

$$C_{36} = \widetilde{W}_3 \otimes \widetilde{W}_3 \otimes \widetilde{W}_4$$

$$48 \times 48 \quad C_{48} = \widetilde{W}_{16} \otimes \widetilde{W}_{3}$$

$$C_{48} = \widetilde{W}_3 \otimes \widetilde{W}_{16}$$

$$64 \times 64 \quad C_{64} = \widetilde{W}_{64}$$

66 Direct sum construction for $N = \sum N_k$

Code matrix $C_N = N \times N$ hybrid orthogonal CDMA code matrix Direct sum construction of C_N

$$C_{\dot{N}} = C_0 \prod_{k>0} \bigoplus C_{N_k}$$

Direct sum definition

 $A = N_a x N_a$ orthogonal code matrix

 $B = N_b x N_b orthogonal code matrix$

 $A \oplus B$ = Direct sum of matrix A and matrix B

= $N_a+N_b \times N_a+N_b$ orthogonal code matrix

$$= \begin{bmatrix} A & O_{N_a x N_b} \\ O_{N_a x N} & B \end{bmatrix}$$

where $O_{N,xN_1} = N_1 x N_1$ zero matrix

It should be obvious to anyone skilled in the communications art that this example implementation of the hybrid complex Walsh in equations (18) clearly defines the fundamental CDMA signal processing relevant to this invention disclosure and it is obvious that this example is representative of the other possible signal processing approaches. For example, the Kronecker matrices E_N and H_N can be replaced by functionals.

For cellular applications the transmitter description which includes equations (18) describes the transmission signal processing applicable to this invention for both the hub and user terminals, and the receiver corresponding to the decoding of equations (18) describes the corresponding receiving signal processing for the hub and user terminals for applicability to this invention.

Walsh CDMA codes and hybrid complex Walsh CDMA codes: It is well known that fast and efficient encoding and decoding algorithms exist for the real Walsh CDMA codes. These are documented in reference [6]. It is obvious that with suitable modifications these algorithms can be used to develop fast and efficient encoding and decoding algorithms for the complex Walsh CDMA codes since these complex codes have real and imaginary code vectors which are from the same set of real Walsh CDMA codes.

It is well known that the Kronecker construction involving DFT and real Walsh orthogonal code vectors have efficient encoding and decoding algorithms. It is obvious that with suitable modifications these algorithms can be used to develop fast and efficient encoding and decoding algorithms for the Kronecker products of DFT and complex Walsh CDMA codes since these complex Walsh codes have real and imaginary code vectors which are from the same set of real Walsh CDMA codes.

Preferred embodiments in the previous description is provided to enable any person skilled in the art to make or use the present invention. The various modifications to these embodiments will be readily apparent to those skilled in the art, and the generic principles defined herein may be applied to other embodiments without the use of the inventive faculty. Thus, the present invention is not intended to be limited to the embodiments shown herein but is not to be accorded the wider scope consistent with the principles and novel features disclosed herein.

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